

أدرب وأحل المسائل

قاعدة السلسلة الأسئلة (1 - 24)

أجد مشتقة كل اقتران مما يأتي:

$$(1) f(x) = e^{4x+2}$$

$$f'(x) = 4e^{4x+2}$$

$$(2) f(x) = 50e^{2x-10}$$

$$f'(x) = 100e^{2x-10}$$

$$(3) f(x) = \cos(x^2 - 3x - 4)$$

$$f'(x) = -(2x - 3) \sin(x^2 - 3x - 4)$$

$$f'(x) = (3 - 2x) \sin(x^2 - 3x - 4)$$

$$(4) f(x) = 10x^2 e^{-x^2}$$

$$f'(x) = (20x) e^{-x^2} + (10x^2) (-2xe^{-x^2}) = 20xe^{-x^2} (1 - x^2)$$

$$(5) f(x) = x + 1x$$

$$f(x) = x + 1x = 1 + 1x$$

$$f'(x) = -1x^{21} + 1x^2 = -12x^2 + 1x$$

$$(6) f(x) = x^2 \tan 1x$$

$$f'(x) = (2x) \tan 1x + (x^2) (\sec^2 1x)$$

$$f'(x) = 2x \tan 1x + x^2 \sec^2 1x$$

$$(7) f(x) = 3x - 5 \cos(\pi x)^2$$

$$f'(x) = 3 + 5(2) (\pi x) (\pi) \sin(\pi x)^2 = 3 + 10\pi^2 x \sin(\pi x)^2$$

$$(8) f(x) = \ln(1 + e^x - e^{-x})$$

$$f(x) = \ln(1 + e^x - e^{-x}) = \ln(1 + e^x) - \ln(1 - e^{-x})$$

$$f'(x) = e^x + e^{-x} + e^x - e^{-x} = 2e^x - e^{-2x}$$

$$(9) f(x) = (\ln x)^4$$

$$f'(x) = 4x (\ln x)^3$$

$$(10) f(x) = \sin x^3 + \sin^3 x$$

$$f'(x) = 3x^2 \cos x^3 + \cos^2 x \sin 2x$$

$$(11) f(x) = x^2 + 8x^5$$

$$f'(x) = 2x + 40x^4$$

$$(12) f(x) = 32x^x$$

$$f'(x) = (x)^{2 \ln 3} 32x - 32x^x 2 = (-1 + 2x \ln 3) 32x^x$$

$$(13) f(x) = 2^{-x} \cos \pi x$$

$$f'(x) = (2^{-x}) (-\pi \sin \pi x) + (\cos \pi x) (-\ln 2) 2^{-x}$$

$$= -\pi 2^{-x} \sin \pi x - 2^{-x} (\cos \pi x) \ln 2$$

$$(14) f(x) = 10 \log_4 x^x$$

$$f'(x) = 10x^x \ln 4 - 10 \log_4 x^x 2 = 10 \ln 4 - 10 \log_4 x^x 2$$

$$(15) f(x) = (\sin x + \cos x)^2$$

$$f'(x) = 2 (\sin x + \cos x) (1 + \cos x) (\cos x) - (\sin x) (-\sin x) (1 + \cos x) 2$$

$$= 2x \sin x + \cos x x (1 + \cos x)$$

$$= 2 \sin x (1 + \cos x) 2$$

$$(16) f(x) = \log_3 (1 + x \ln x)$$

$$f'(x) = \frac{1}{1 + \ln x (\ln 3)} \left(\ln x + (1 + x \ln x) \cdot \frac{1}{x} \right) = \frac{1 + \ln x (\ln 3) + 1 + x \ln x}{1 + \ln x (\ln 3) (1 + x \ln x)}$$

$$(17) f(x) = e^{\sin 2x} + \sin (e^{2x})$$

$$f'(x) = 2e^{\sin 2x} \cos 2x + 2e^{2x} \cos (e^{2x})$$

$$(18) f(x) = \tan^4 (\sec (\cos x))$$

$$f'(x) = 4(\tan (\sec (\cos x)))^3 \sec^2 (\sec (\cos x)) \times \sec (\cos x) \tan (\cos x) \times (-\sin x)$$

$$= -4 \tan^3 (\sec (\cos x)) \sec^2 (\sec (\cos x)) \sec (\cos x) \tan (\cos x) \sin x$$

x أجد معادلة المماس لكل اقتران ممّا يأتي عند قيمة المعطاة:

$$(19) f(x) = 4e^{-0.5x^2}, x = -2$$

$$f(x) = 4e^{-0.5x^2} \quad f(-2) = 4e^{-0.5(-2)^2} = 4e^{-2} \quad f'(x) = -4xe^{-0.5x^2}$$

ميل المماس هو:

$$m = f'(-2) = -4(-2)e^{-0.5(-2)^2} = 8e^{-2}$$

معادلة المماس هي:

$$y - 4e^{-2} = 8e^{-2}(x + 2) \rightarrow y = 8e^{-2}x + 20e^{-2}$$

$$(20) f(x) = x + \cos 2x, x = 0$$

$$f(x) = x + \cos 2x \quad f(0) = 0 + \cos(0) = 1 \quad f'(x) = 1 - 2\sin 2x$$

ميل المماس هو:

$$m = f'(0) = 1 - 2\sin 2(0) = 1$$

معادلة المماس هي:

